

Plumas beta lineales forzadas por el viento: aplicaciones a la Contracorriente Hawaiana

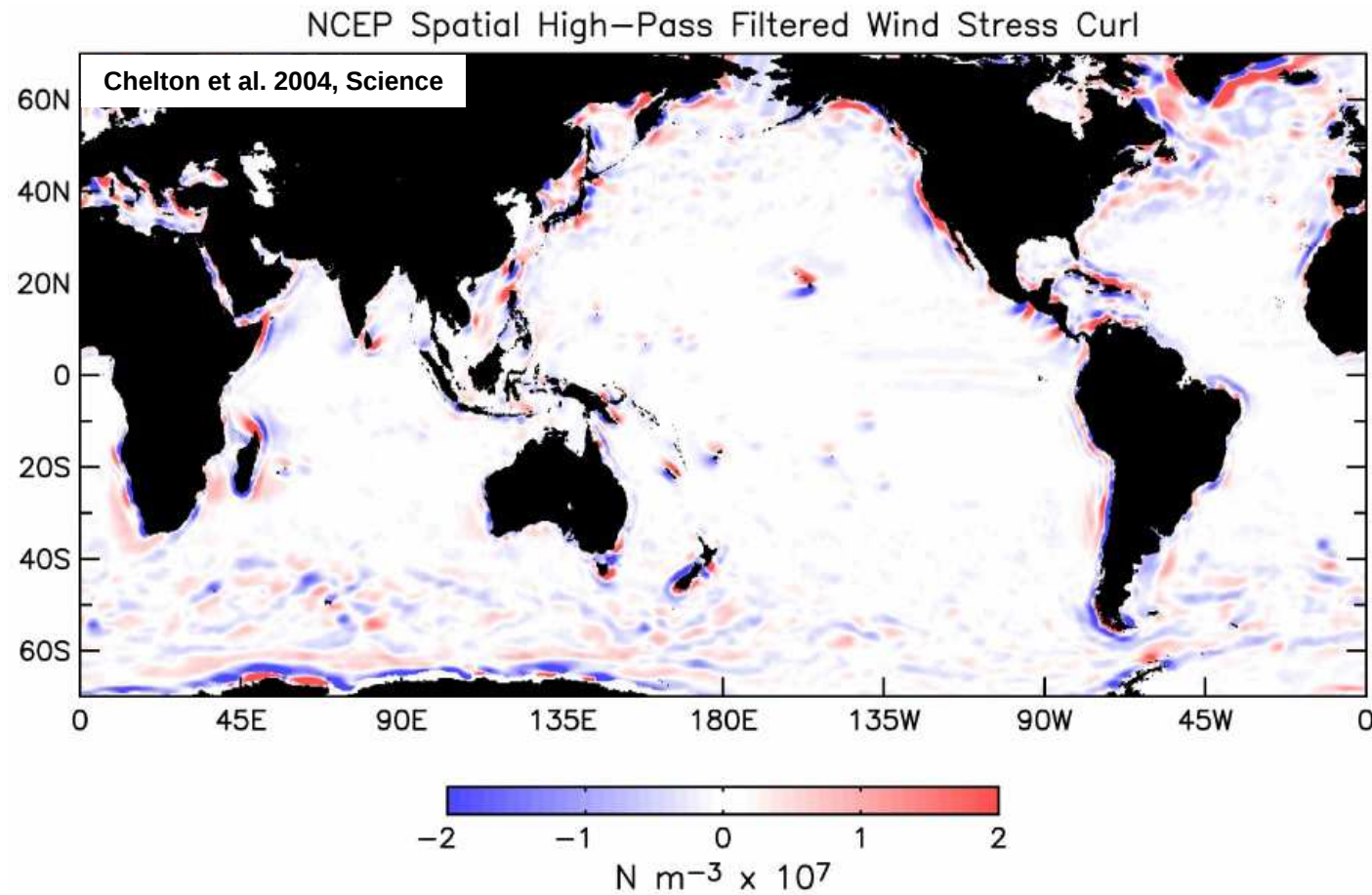
Ali Belmadani^{1,2}

J. Phys. Oceanogr., accepted

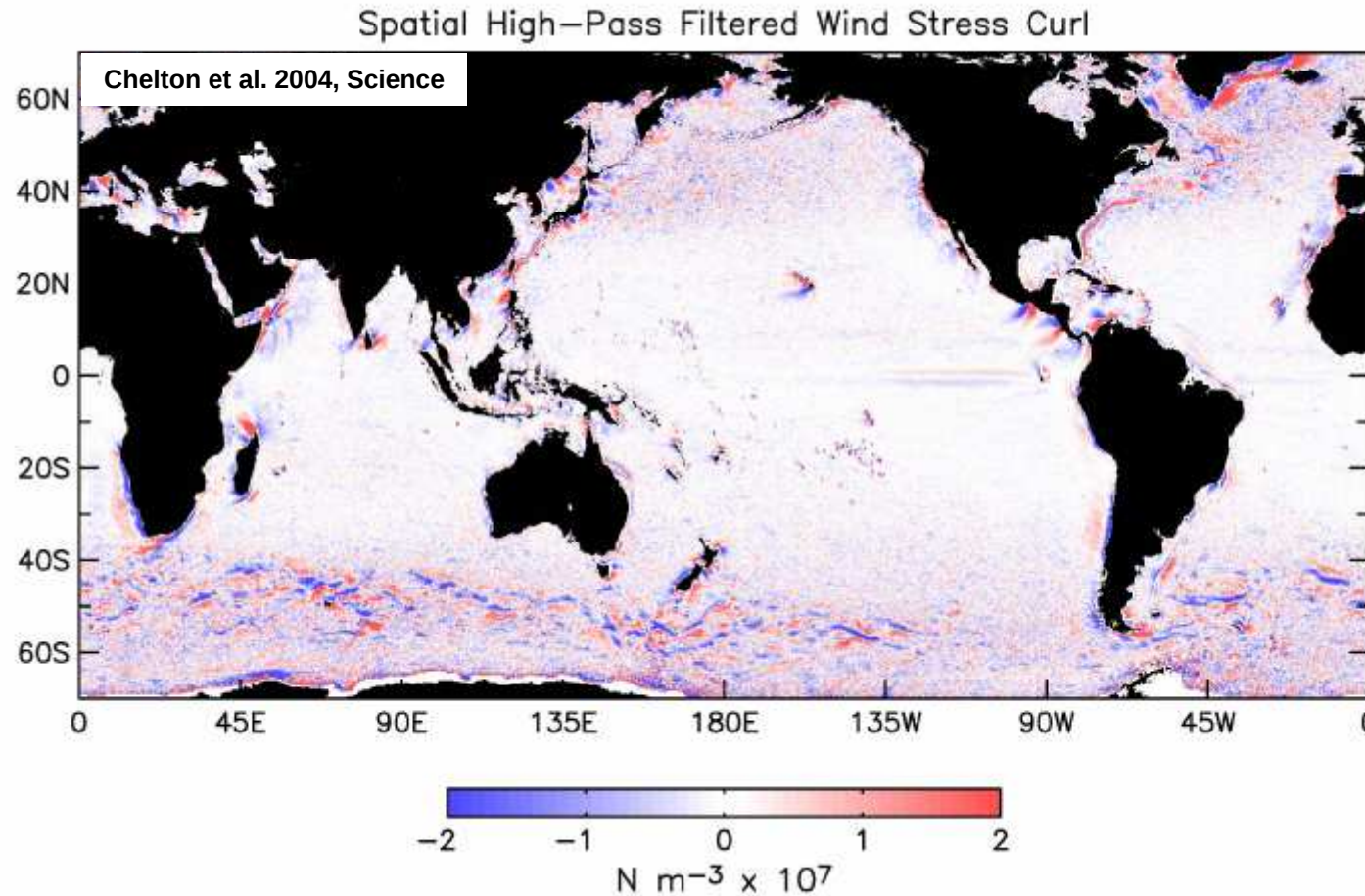
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Small-scale wind stress curl (WSC)

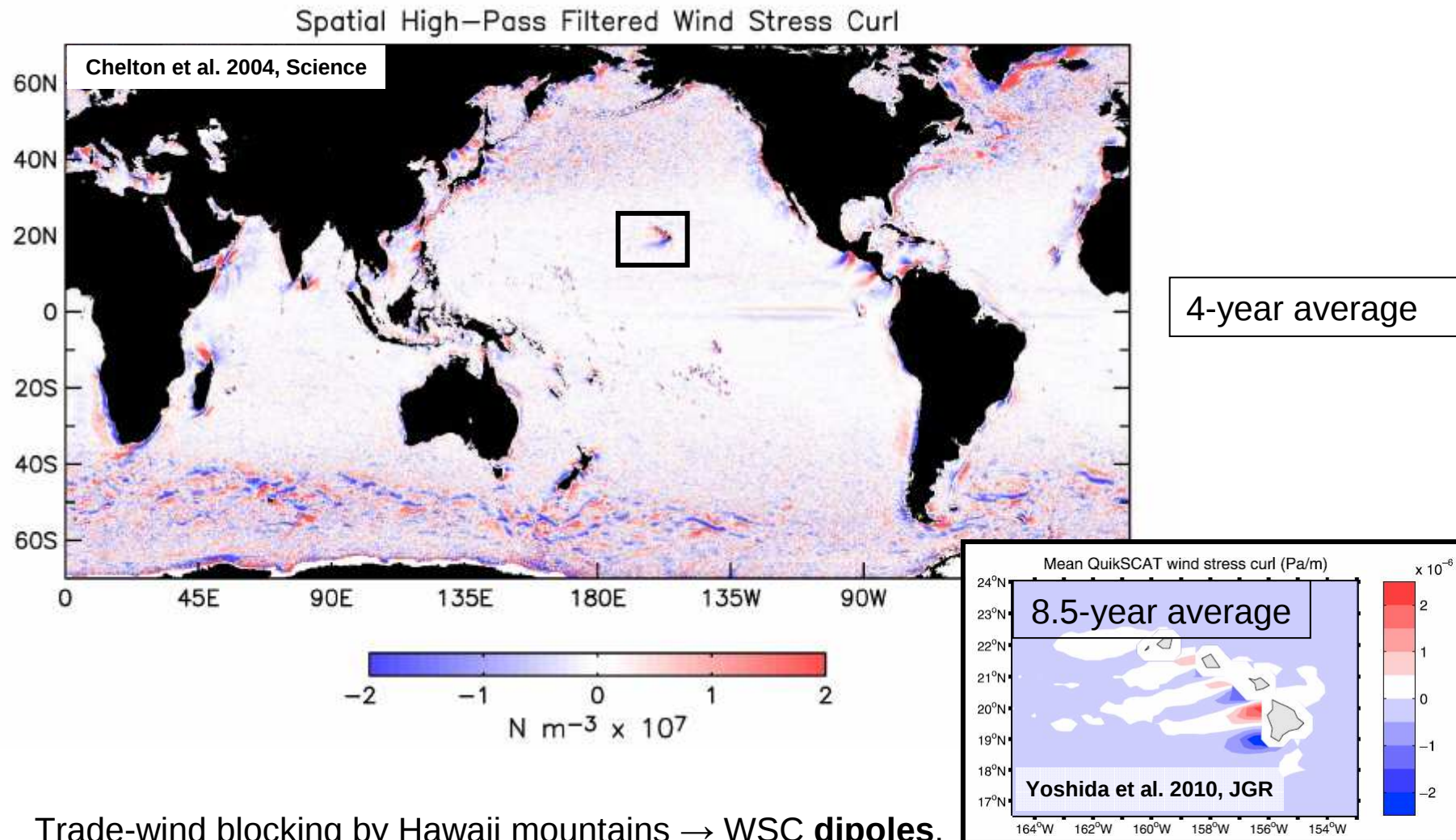


Small-scale wind stress curl (WSC)



- **Persistent small-scale WSC:** fronts, currents, orography (e.g., tall islands).
- **Patterns:** dipoles, monopoles, bands, etc.
- **Ocean dynamical response?**

Ocean response: example of the Hawaiian Lee Countercurrent (HLCC)

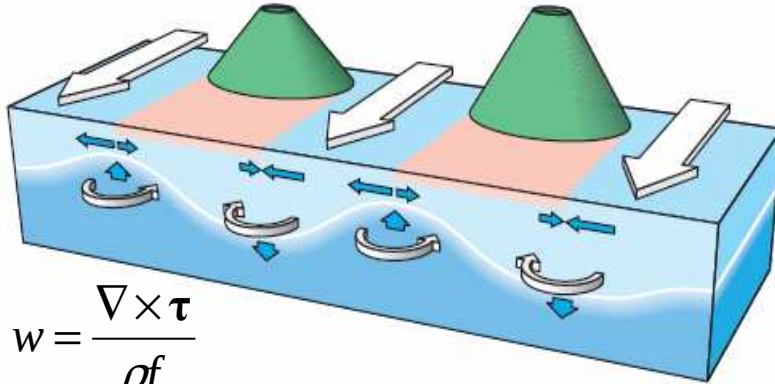


- Trade-wind blocking by Hawaii mountains → WSC **dipoles**.
- Dipole in Big Island lee drives **HLCC** via **Sverdrup** dynamics (e.g., Xie et al. 2001, Science).

HLCC: curl-driven zonal jet

Ekman flow: w

Chavanne et al. 2002, CJRS



$$w = \frac{\nabla \times \tau}{\rho f}$$

Ekman pumping

- **WSC** drives **Ekman pumping** / suction.
- **Thermocline** is lifted / depressed.
- Cyclonic / anticyclonic **eddies** (e.g., Calil et al. 2008, DSR).
- **Rossby waves** propagate anomalies (e.g., Sasaki et al. 2010, OD).

Sverdrup flow: V

$$\frac{\partial \xi}{\partial t} + \beta v = f \frac{\partial w}{\partial z} + \frac{1}{\rho} \frac{\partial \nabla \times \tau}{\partial z}$$

Baroclinic Vorticity Equation

- Vorticity produced by **vortex stretching** + **planetary vorticity** + **turbulent stress**.
- **Barotropic vorticity equation** (flat bottom): vortex stretching vanishes.

$$V = \frac{\nabla \times \tau}{\rho \beta}$$

Sverdrup Balance

- **Meridional transport** driven by **WSC** (at steady state).

Volume conservation: U

$$\frac{\partial U}{\partial x} + \frac{\partial V}{\partial y} = 0$$

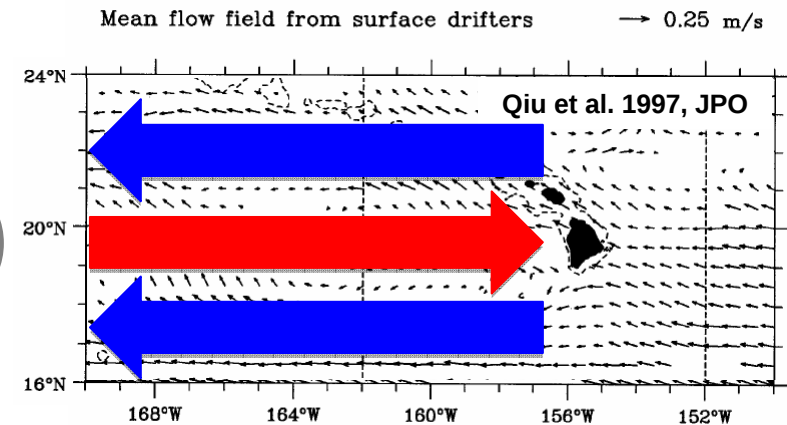
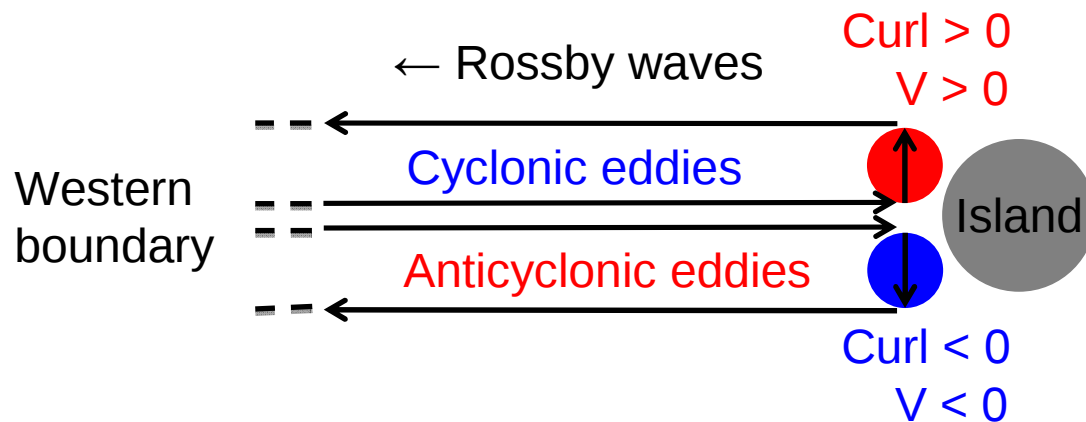
Barotropic Continuity Equation

- **Nondivergent barotropic flow**.
- **Zonal transport to the west**.

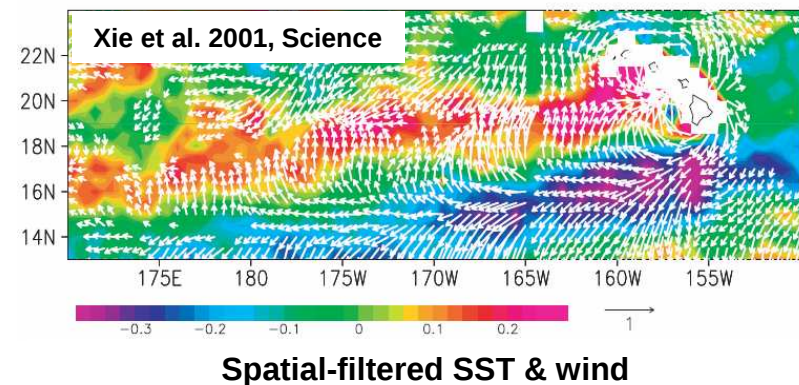
$$U = - \int_{x_e}^x \frac{\partial V}{\partial y} dx$$

Integration from eastern boundary

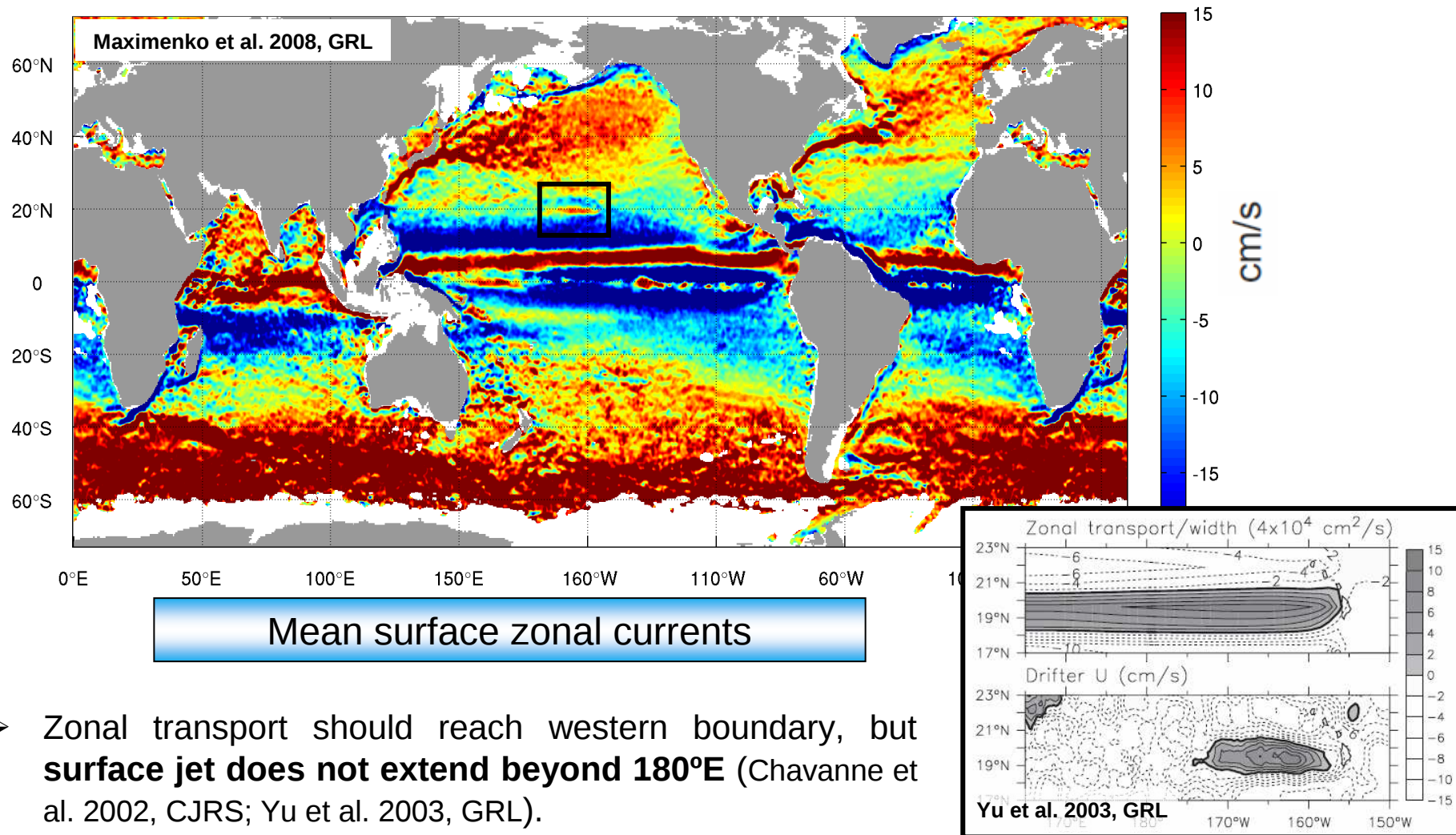
HLCC: wind-forced β -plume



- **Elongated double-gyre** west of Hawaii.
- **HLCC: narrow eastward jet** embedded in broad North Equatorial Current (NEC).
- **β -plume** (Rhines 1994, Chaos) = **Sverdrup gyre** driven by **compact vorticity source** (momentum, heat, mass).
- **HLCC = wind-forced β -plume** (Jia et al. 2011, JGR).
- **Other mechanisms: air-sea coupling**, island-induced modified large-scale flow (Qiu Durland 2002, JPO), mode water intrusions (Sasaki et al. 2012, JO), etc.
- HLCC advects warm SST → **far-field WSC dipole** (Xie et al. 2001, Science; Hafner Xie 2003, JAS; Sakamoto et al. 2004, GRL; Sasaki Nonaka 2006, GRL, etc.).



HLCC early termination



- Zonal transport should reach western boundary, but **surface jet does not extend beyond 180°E** (Chavanne et al. 2002, CJRS; Yu et al. 2003, GRL).
- **Horizontal dissipation by mesoscale eddies** → HLCC early termination (Yu et al. 2003).
- Underlying assumption: **equivalent-barotropic** vertical structure.

$$u(z) = \frac{U}{d_{th}} e^{z/d_{th}}$$

Chavanne et al. 2002, CJRS

Baroclinic β -plumes and the HLCC

- What is the **baroclinic structure** of β -plumes induced by localized WSC? HLCC?
- What is the **sensitivity** of the ocean circulation to the **scale of the WSC forcing**? HLCC?
- **Are eddies necessary** for the early termination of β -plumes? HLCC?

Outline

1. **Linear baroclinic β -plumes:** idealized model and theory

2. **HLCC vertical structure:** model results and observations

Conclusion

Idealized wind-forced β -plume: model set-up

- **ROMS** (Shchepetkin McWilliams 2005, OM): free surface, hydrostatic model, resolves the primitive equations using stretched σ -coordinates.
- **Idealized subtropical ocean** (20°N - 40°N, 60° zonal) with **flat bottom** (H=4000m).
- **Eddy-resolving** (1/12°) with **32 vertical levels**.
- **Uniform initial stratification** $N^2(z)$ from World Ocean Atlas 2009 (typical of N Pacific gyre).
- **Constant vertical diffusion + viscosity**: $\kappa=10^{-5}\text{m}^2\text{s}^{-1}$, $\nu=10^{-4}\text{m}^2\text{s}^{-1}$.
- Simulation started from rest and run for **30 years** with 20 min time step (20 s for the barotropic mode). **Steady state after 20 years**. Outputs are saved every 5 days.
- Surface forcing: **localized steady wind vortex** in the center of the domain
→ **WSC quasi-monopole** (basic physics).
- **Linear regime**: weak wind $\tau_{\text{max}}=10^{-5}\text{Nm}^{-2}$.

Linear β -plume: steady-state barotropic solution

Wind: steady anticyclonic vortex ($R = 40$ km)

$$\psi_a = R\tau_{\max} \sqrt{e} \exp\left(-\frac{x^2 + y^2}{2R^2}\right), \quad \boldsymbol{\tau} = \mathbf{k} \times \nabla \psi_a$$

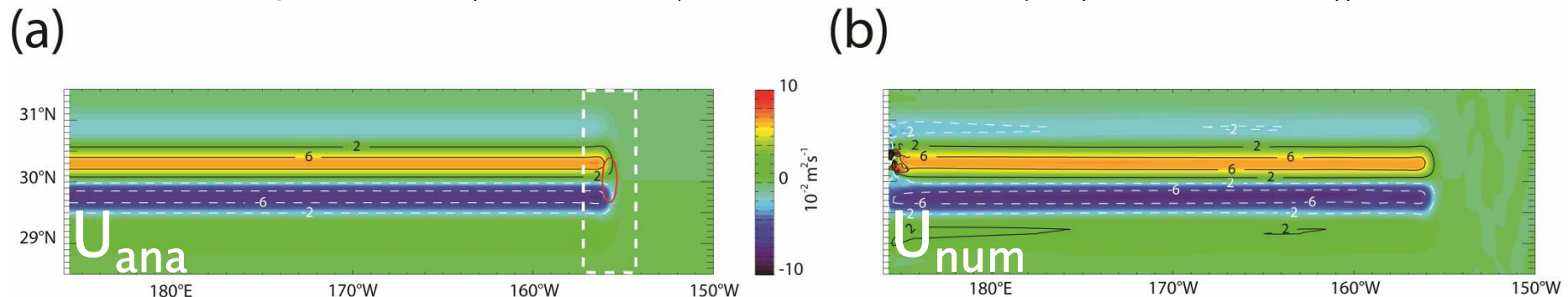
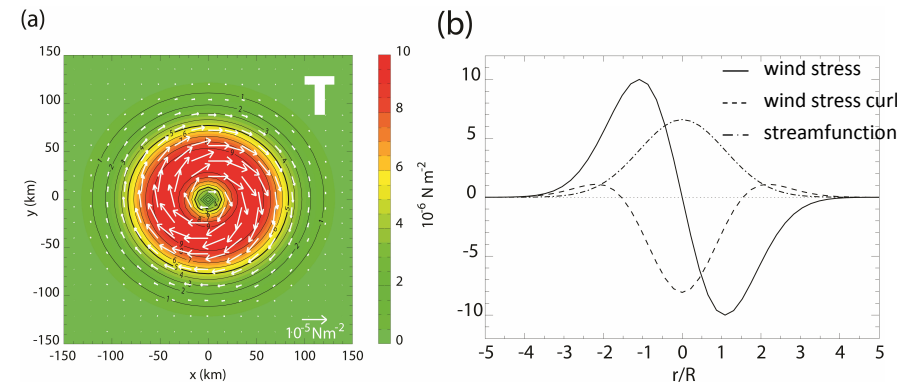
Meridional transport: Sverdrup balance

$$\bar{V} = \frac{\nabla \times \boldsymbol{\tau}}{\rho\beta}, \quad \rho = 1025 \text{ kg.L}^{-1}$$

$$\beta \approx 1.98 \cdot 10^{-11} \text{ s}^{-1}\text{m}^{-1}$$

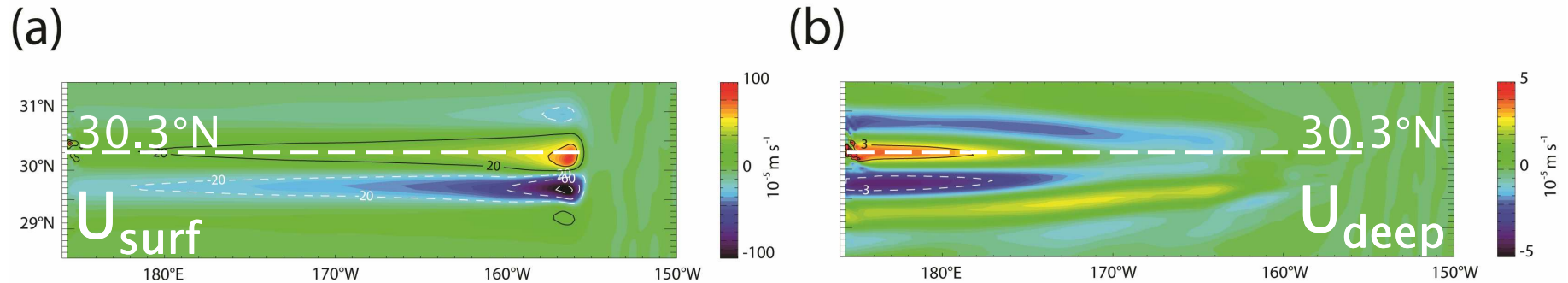
Zonal transport: continuity equation

$$\bar{U} = -\int_{x_e}^x \frac{\partial \bar{V}}{\partial y} dx = \frac{\tau_{\max} \sqrt{e}}{\rho R^4 \beta} y \cdot e^{-\frac{y^2}{2R^2}} \left\{ \sqrt{\frac{\pi}{2}} (3R^2 - y^2) \left[\operatorname{erf}\left(\frac{x_e}{\sqrt{2}R}\right) - \operatorname{erf}\left(\frac{x}{\sqrt{2}R}\right) \right] - R \left[x \cdot e^{-\frac{x^2}{2R^2}} - x_e \cdot e^{-\frac{x_e^2}{2R^2}} \right] \right\}, \quad x_e \approx 2890 \text{ km}$$



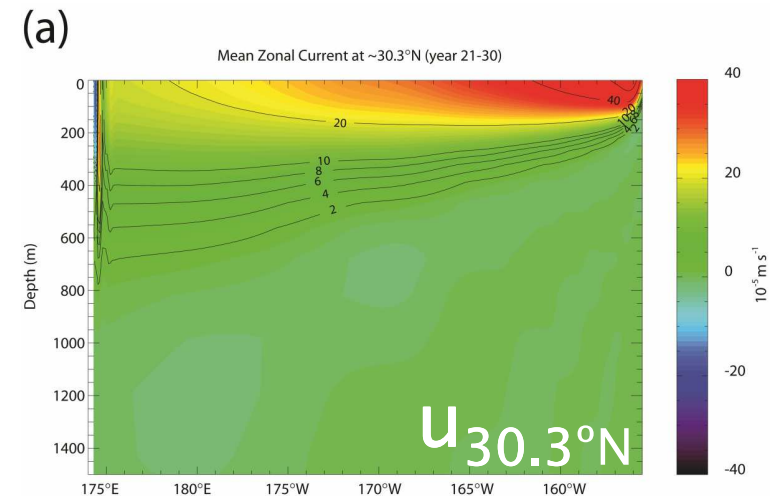
- **Good agreement** between analytical and numerical solutions.
- **1 anticyclonic cell (2 jets) + 2 weak cyclonic cells = 2+2 x-independent zonal jets.**

Linear β -plume: Vertical structure



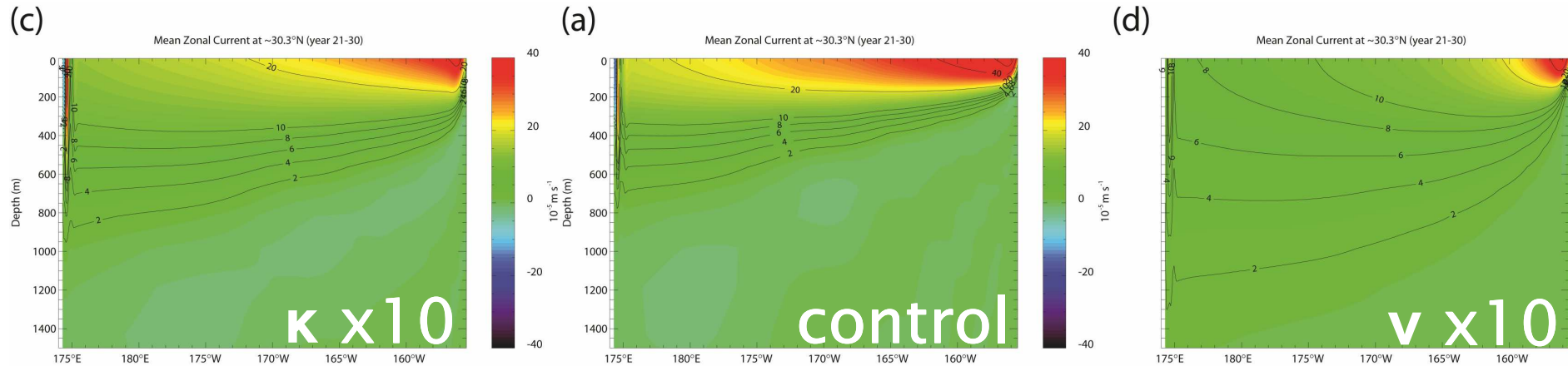
- In contrast with barotropic flow, **surface jets decay westward.**

- **Deepening of β -plume** lower boundary + emergence of **deep flow far away from forcing.**



- Zonal change in baroclinic structure: **damping of baroclinic Rossby waves?** (especially higher-order modes)

Linear β -plume: Vertical mixing effects



- Zonal scales are smaller when vertical mixing is increased.
- Stronger sensitivity to viscosity compared to diffusion.
- Usually vertical viscosity effects are very weak. Why are they dominant here?

Linear continuously-stratified (LCS) model

Linearized primitive equations (McCreary 1981, PTRa)

$$\begin{aligned}\frac{\partial u}{\partial t} - fv + \frac{1}{\rho_0} \frac{\partial p}{\partial x} &= \frac{\partial}{\partial z} \left(\nu \frac{\partial u}{\partial z} \right) & \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} &= 0 \\ \frac{\partial v}{\partial t} + fu + \frac{1}{\rho_0} \frac{\partial p}{\partial y} &= \frac{\partial}{\partial z} \left(\nu \frac{\partial v}{\partial z} \right) & \frac{\partial p}{\partial z} &= -\rho g \\ \frac{\partial \rho}{\partial t} - \frac{\rho_0 N^2}{g} w &= \frac{\partial^2}{\partial z^2} (\kappa \rho)\end{aligned}$$

Vertical mode decomposition

$$\begin{aligned}u(x, y, z, t) &= \sum_{n=1}^{+\infty} u_n(x, y, t) \psi_n(z) & w(x, y, z, t) &= \sum_{n=1}^{+\infty} w_n(x, y, t) \int_{-H}^z \psi_n(z) dz \\ v(x, y, z, t) &= \sum_{n=1}^{+\infty} v_n(x, y, t) \psi_n(z) & \rho(x, y, z, t) &= \sum_{n=1}^{+\infty} \rho_n(x, y, t) \frac{\partial \psi_n(z)}{\partial z} \\ p(x, y, z, t) &= \sum_{n=1}^{+\infty} p_n(x, y, t) \psi_n(z)\end{aligned}$$

$$\frac{\partial}{\partial z} \left(\frac{1}{N^2(z)} \frac{\partial \psi_n(z)}{\partial z} \right) = -\frac{1}{c_n^2} \psi_n(z)$$

Linear continuously-stratified (LCS) model (2)

Steady-state **baroclinic mode primitive equations** (McCreary 1981, PTR)A)

$$\frac{\nu N^2}{c_n^2} u_n - f v_n + \frac{1}{\rho_0} \frac{\partial p_n}{\partial x} = F_n$$

$$\frac{\nu N^2}{c_n^2} v_n + f u_n + \frac{1}{\rho_0} \frac{\partial p_n}{\partial y} = G_n$$

$$\frac{\kappa N^2}{\rho_0 c_n^4} p_n + \frac{\partial u_n}{\partial x} + \frac{\partial v_n}{\partial y} = 0$$

$$w_n = -\frac{\kappa N^2}{\rho_0 c_n^4} p_n$$

$$p_n = -\rho_n g$$

$$, F_n = \tau_x / \rho_0 \int_{-H}^0 \psi_n^2 dz$$

$$, G_n = \tau_y / \rho_0 \int_{-H}^0 \psi_n^2 dz$$

Steady-state baroclinic mode **quasi-geostrophic potential vorticity equation**

$$\beta \frac{\partial p_n}{\partial x} = \frac{\kappa N^2 f^2}{c_n^4} p_n - \frac{\nu N^2}{c_n^2} \left(\frac{\partial^2 p_n}{\partial x^2} + \frac{\partial^2 p_n}{\partial y^2} \right) + \rho_b f \left(\frac{\partial G_n}{\partial x} - \frac{\partial F_n}{\partial y} \right)$$

β effect

Vortex stretching

Curl (viscosity)

WSC

Linear continuously-stratified (LCS) model (3)

- Ratio of K -term [*Vortex stretching*] over V -term [*Curl(viscosity)*]:

$$M_n = \frac{\kappa f^2}{c_n^2} p_n \bigg/ \nu \left(\frac{\partial^2 p_n}{\partial x^2} + \frac{\partial^2 p_n}{\partial y^2} \right) \sim \frac{\kappa f^2}{c_n^2} \bigg/ \nu \left(\frac{1}{L_x^2} + \frac{(2\pi)^2}{L_y^2} \right) \approx \frac{\kappa f^2 L_y^2}{4\pi^2 \nu c_n^2} = \frac{4R^2}{\pi^2 \sigma R_n^2}$$

with $\sigma = \frac{\nu}{\kappa}$ (Prandtl number), $R_n = \frac{c_n}{f} = \frac{c_1}{nf}$ (Rossby radius), and $L_y = 4R$ (y-wavelength)

- For **large-scale flow**, $R \gg R_n$ $\pi\sqrt{\sigma}/2$ and $M_n \gg 1$:

$$\Rightarrow \quad \beta \frac{\partial p_n}{\partial x} = \frac{\kappa N^2 f^2}{c_n^4} p_n + \rho_b f \left(\frac{\partial G_n}{\partial x} - \frac{\partial F_n}{\partial y} \right)$$

*Vortex
stretching*

- For **small-scale WSC**, $R \ll R_n$ $\pi\sqrt{\sigma}/2$ and $M_n \ll 1$:

$$\Rightarrow \quad \beta \frac{\partial p_n}{\partial x} = -\frac{\nu N^2}{c_n^2} \left(\frac{\partial^2 p_n}{\partial x^2} + \frac{\partial^2 p_n}{\partial y^2} \right) + \rho_b f \left(\frac{\partial G_n}{\partial x} - \frac{\partial F_n}{\partial y} \right)$$

Curl (viscosity)

Baroclinic mode damping by viscosity/diffusion

Viscosity vs. Diffusion: dependence on mode number

$$M_n = \frac{4R^2}{\pi^2 \sigma R_1^2} n^2 = M_1 n^2 \quad \Rightarrow \quad \text{Even when } M_1 \ll 1, \text{ for } n \geq n_0 \text{ high enough } M_n \geq 1$$

- For **small-scale WSC**, viscosity (diffusion) damps the lower- (higher-) order modes
 - ↳ In ROMS, $M_1 \approx 0.04$ and $n_0 \approx 6$ **explain the stronger sensitivity to viscosity**
- For **large-scale flow**, diffusion damps all the baroclinic modes

Viscosity vs. Diffusion: decay length scales

- Viscosity:

$$L_v = \frac{4\beta R^2 c_1^2}{\pi^2 \nu n^2 N^2}$$

- Diffusion:

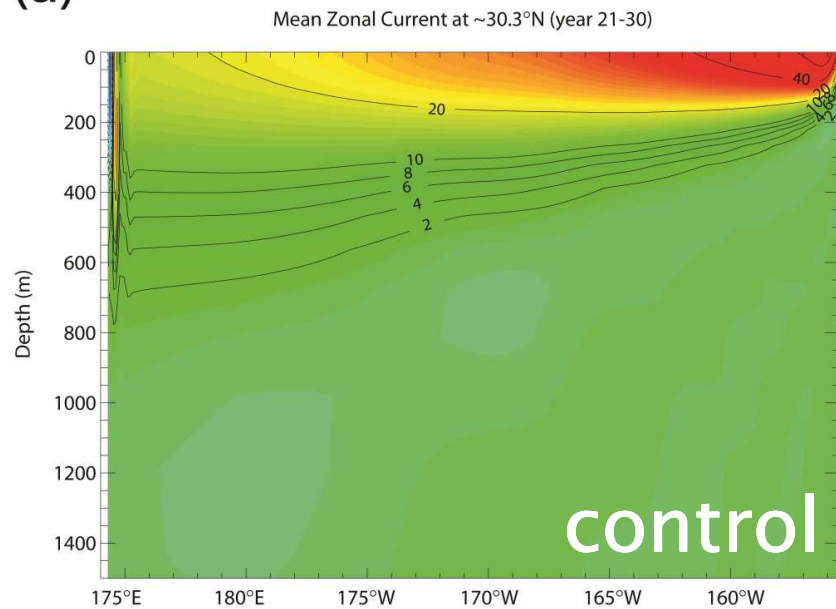
$$L_\kappa = \frac{\beta c_1^4}{\kappa f^2 n^4 N^2}$$

- Smaller scales with enhanced mixing.
- Smaller scales for higher-order modes.
- **Only L_v varies with R** because *Curl(viscosity)* acts on vorticity perturbation while *Vortex stretching* acts on pressure perturbation.

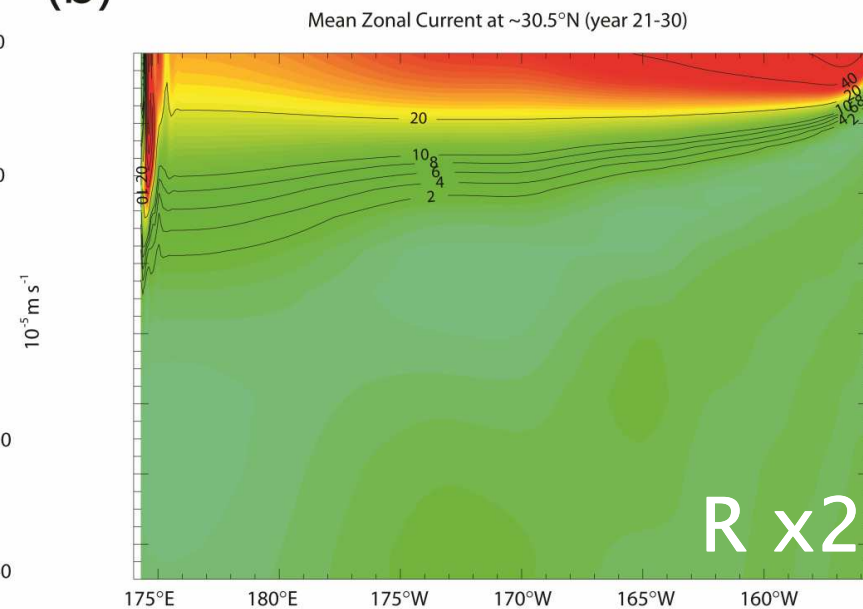
Sensitivity to forcing scale

Wind: $R \times 2$, $T_{\max} \times 2$

(a)



(b)



$$L_v = \frac{4\beta R^2 c_1^2}{\pi^2 \nu n^2 N^2}$$

- Baroclinic x-scale increases with WSC y-scale in agreement with theory.

Outline

1. Linear baroclinic β -plumes: idealized model and theory

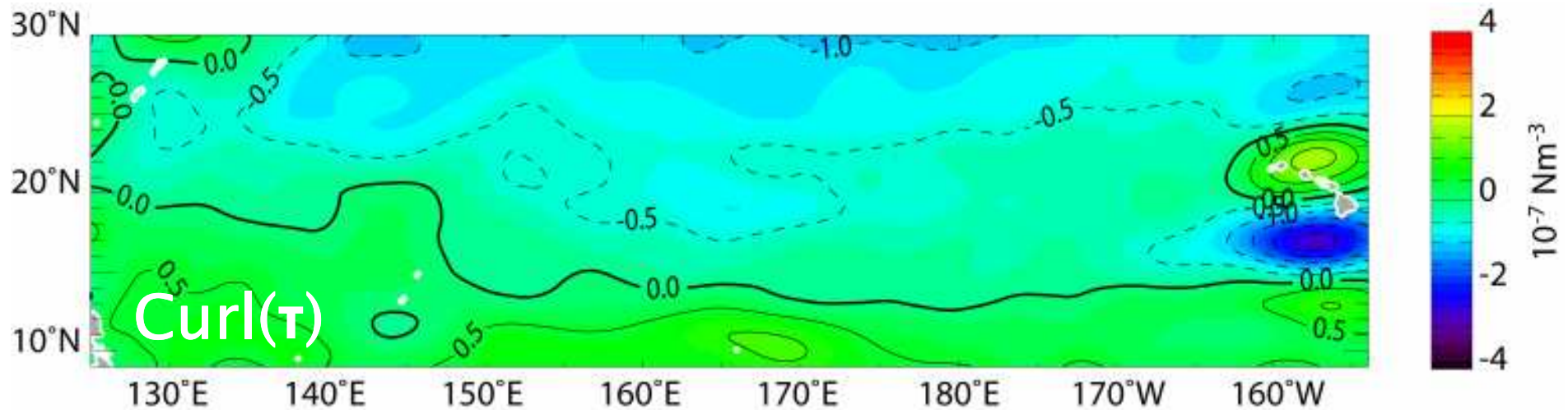
2. **HLCC vertical structure**: model results and observations

Conclusion

Hawaiian Lee Countercurrent: model and data

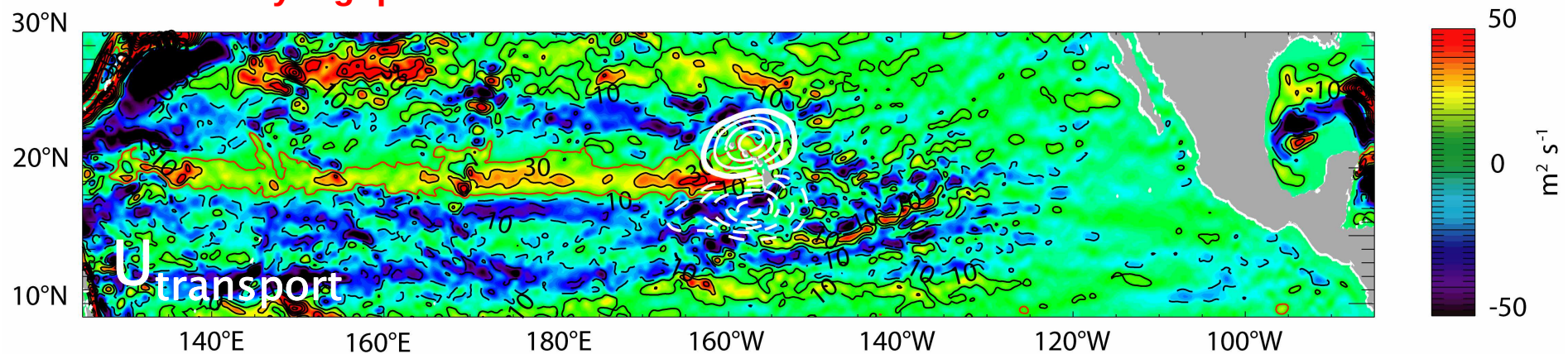
- **OFES** (Masumoto et al. 2004, JES): **global ocean model** based on GFDL MOM3.
- **Eddy-resolving** ($1/10^\circ$) with **54 vertical levels**. **Bottom topography** is from OCCAM $1/30^\circ$.
- **KPP vertical mixing** scheme (Large et al. 1994, RG).
- **Study region = (sub)tropical North Pacific Ocean** ($9^\circ\text{N} - 30^\circ\text{N}$, $125^\circ\text{E} - 85^\circ\text{W}$).
- **2 simulations** analyzed over 1999-2008 (**10 years**): **OFES-N** (NCEP forcing) and **OFES-Q** (QuikSCAT forcing), similarly to Sasaki Nonaka 2006, GRL. Monthly means are used here.
- Lebedev et al. 2007, IPRC = **surface** and **deep currents** estimated from trajectories of 4284 **ARGO** floats over 1997-2007 (**11 years**).
- **Surface velocities** = linearly regressed from float coordinates fixed by satellite.
- **Deep velocities** estimated from float displacements during submerged phase of the cycle.

HLCC in OFES: NCEP forcing



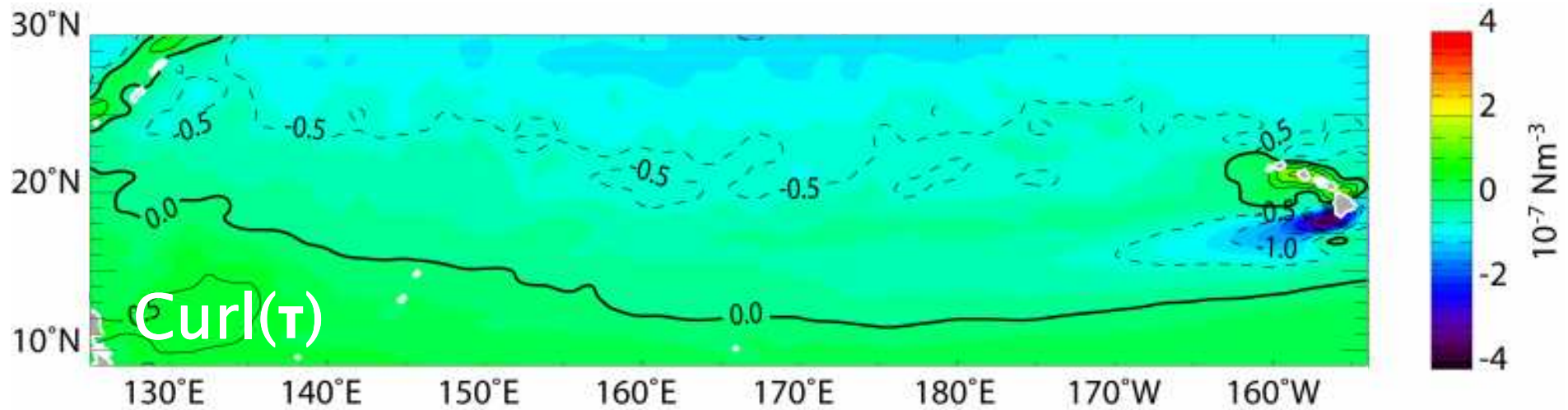
(a)

Meridionally highpass filtered



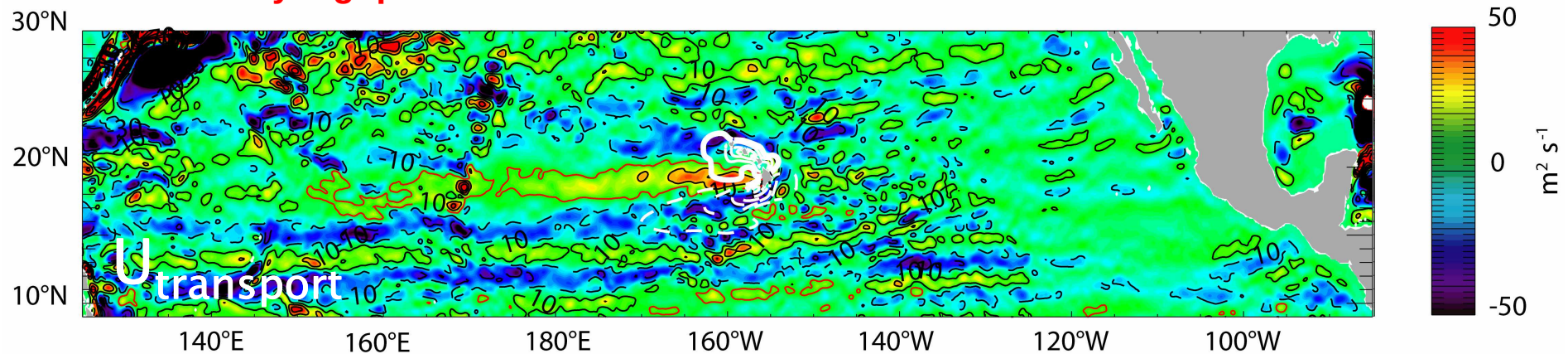
- HLCC = β -plume forced by WSC dipole around Hawaii.
- Transport is $\sim x$ -independent (at least east of 170°E).

HLCC in OFES: QuikSCAT forcing



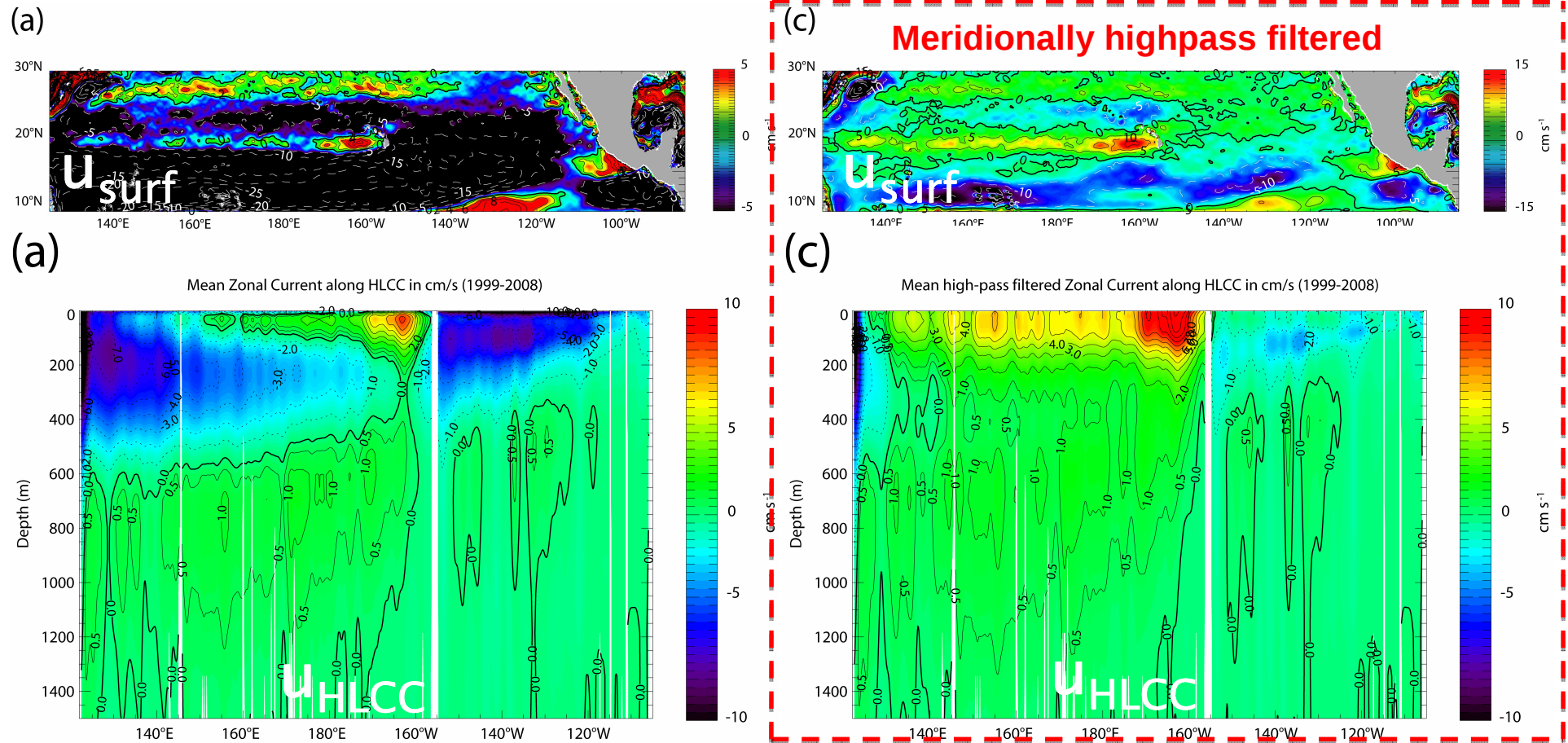
(b)

Meridionally highpass filtered



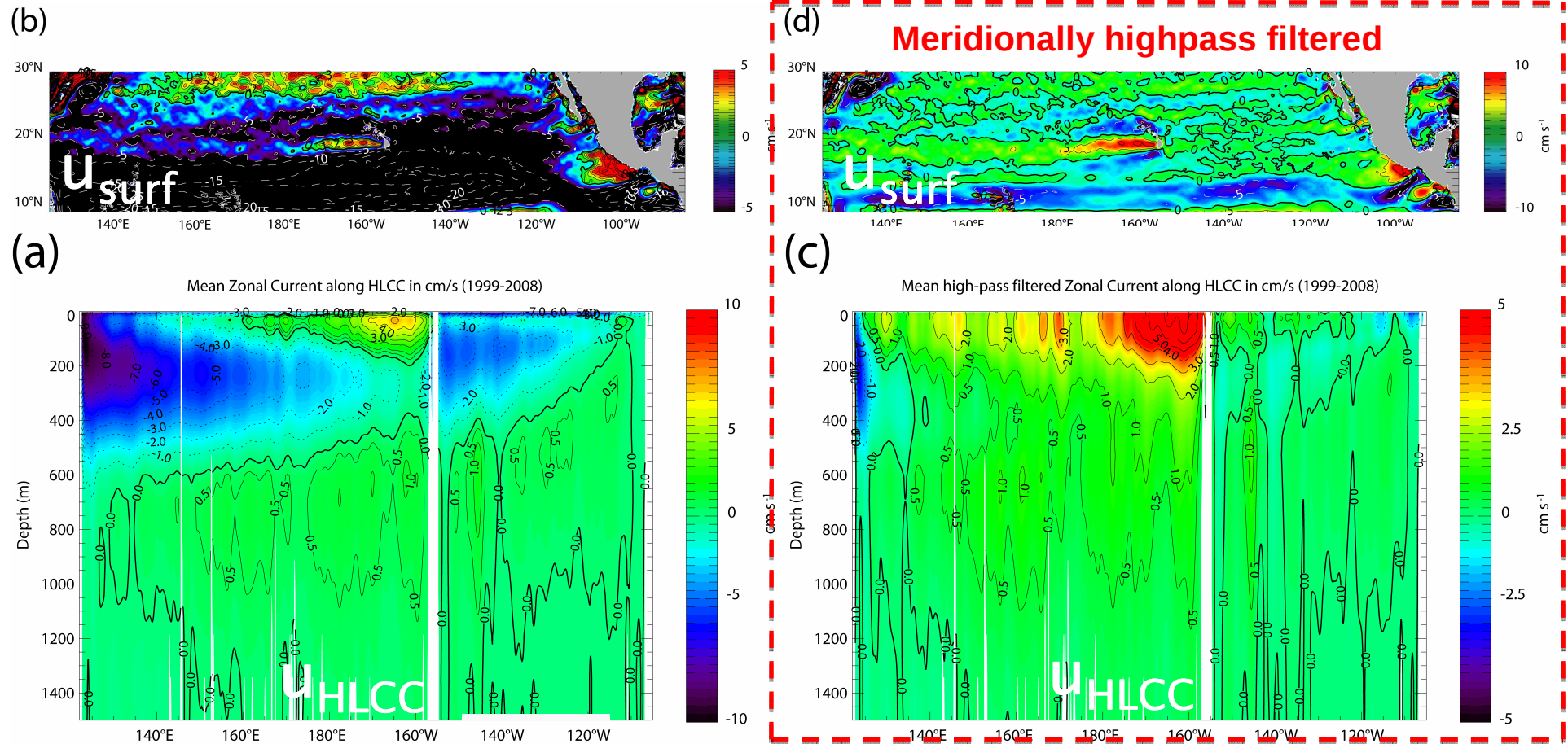
- Forcing scale = smaller $\Rightarrow$ narrower HLCC meridional scale.
- Transport also decays: due to far-field wind or eddy dissipation?

HLCC in OFES: NCEP forcing



- **Surface current** extends to **~155°E**, but **weaker west of ~170°W**.
- **Baroclinic flow** = NEC + **β -plume**: surface decay, westward deepening, emergence of deep flow.

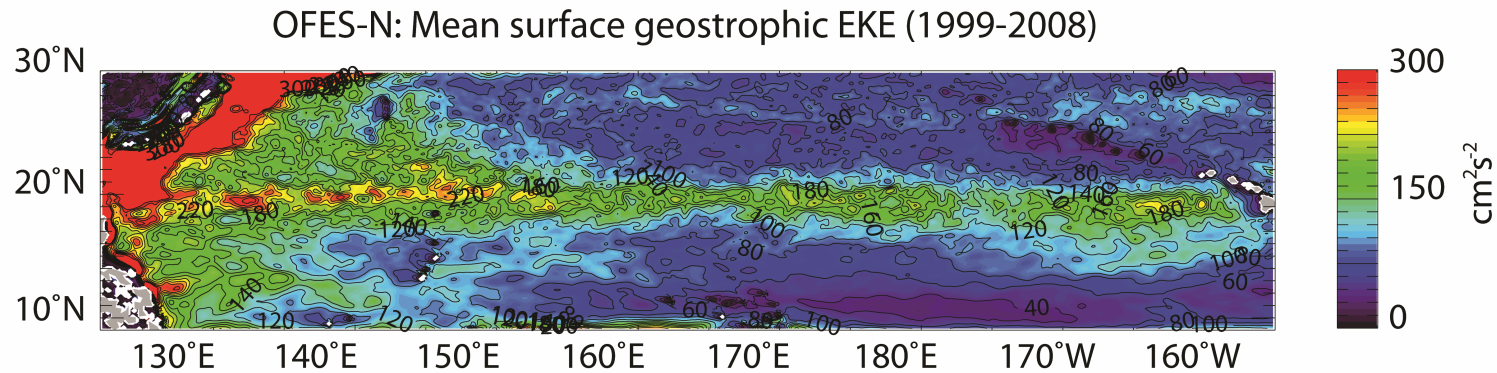
HLCC in OFES: QuikSCAT forcing



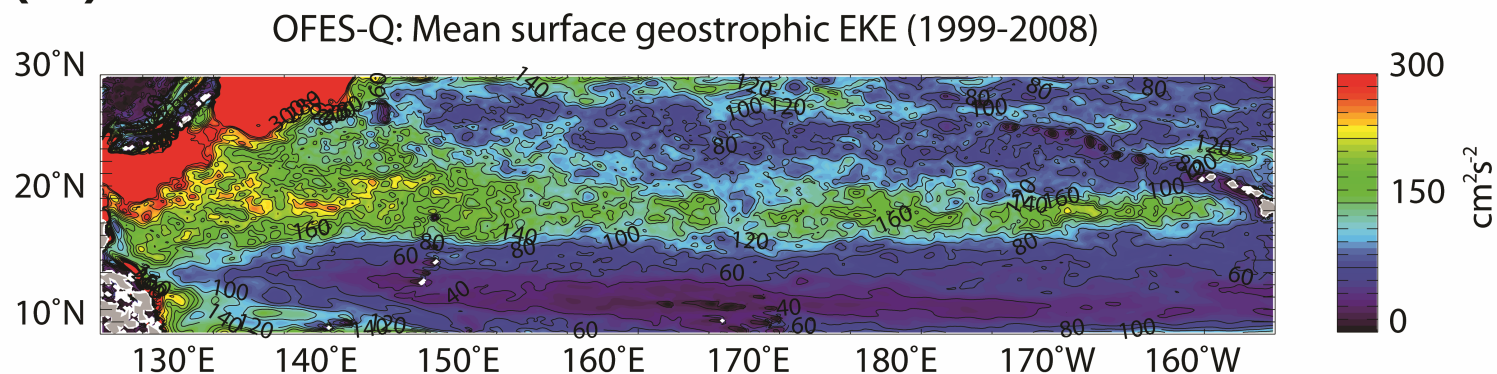
- **Surface current decay scale = shorter:** consistent with idealized model.
- **Baroclinic flow: less consistent** with idealized β -plume. Due to eddies and/or far-field wind?

Transport decay: eddies?

(a)

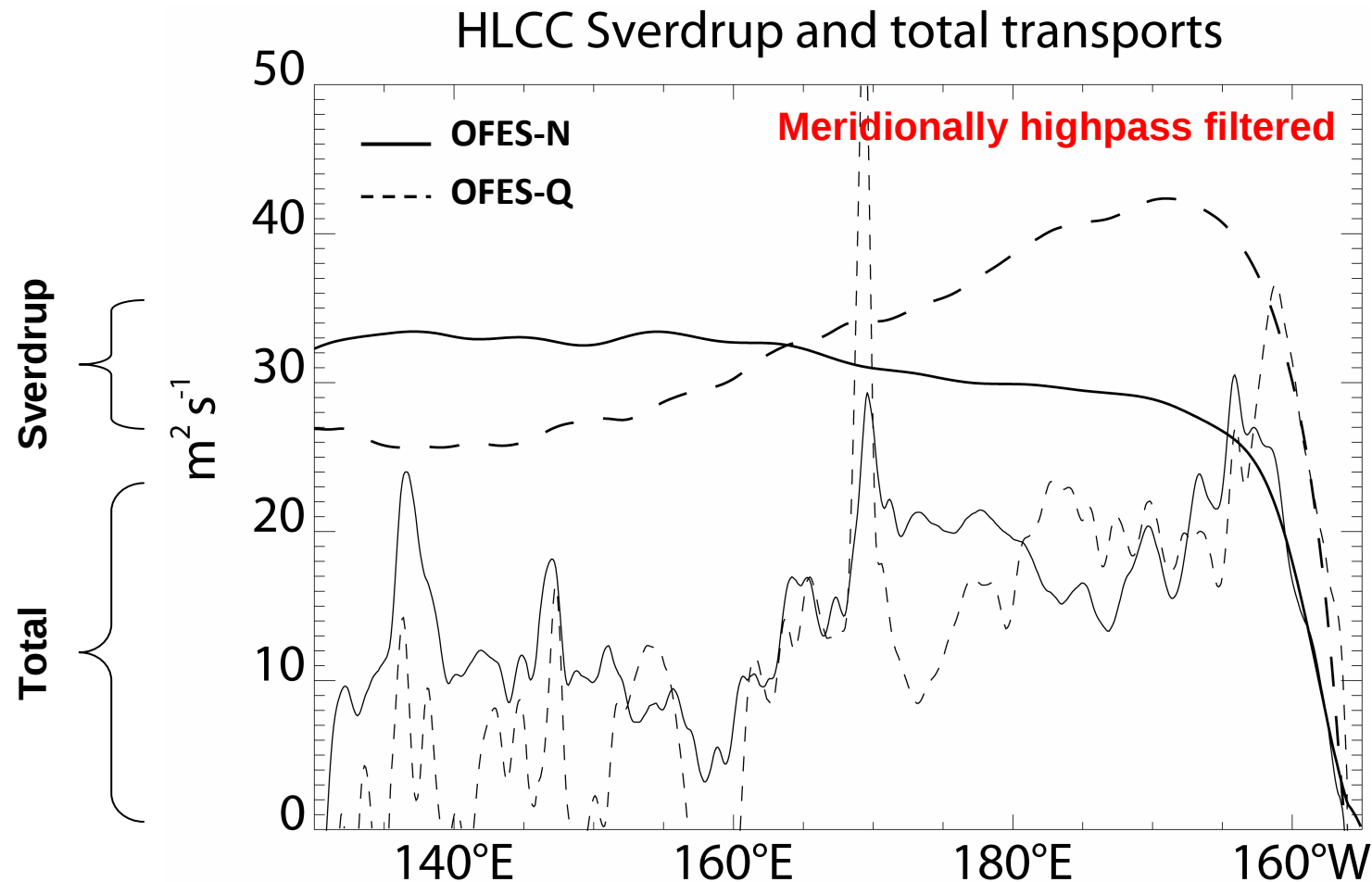


(b)



- **High EKE along the HLCC axis** due to eddies shed in the island lee and generated by baroclinic/barotropic instabilities in the far field (Calil et al. 2008, Yoshida et al. 2011, etc.).
- **Similar EKE levels in OFES-N/Q** (slightly higher in OFES-N) suggest **eddies may not be responsible** for differences in barotropic transport.

Transport decay: Sverdrup flow?



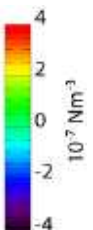
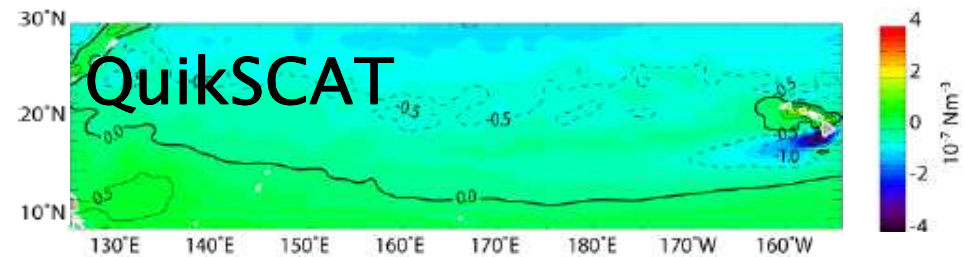
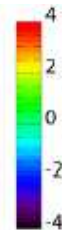
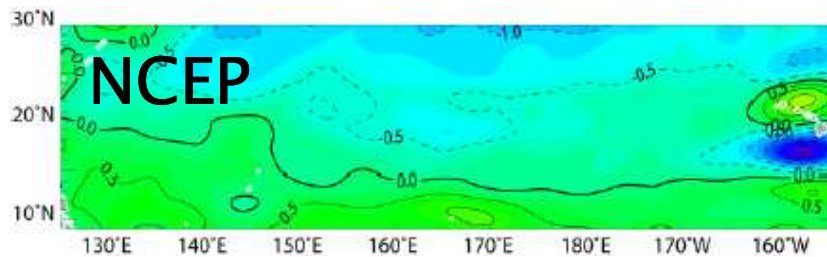
- NCEP WSC favors an $\sim x$ -independent transport west of Hawaii, whereas **QuikSCAT WSC likely contributes to the faster-decaying transport.**
- This is likely due to the effect of **air-sea interaction** in the far field with **tilted WSC dipole and HLCC**. Possibly also contributes to **discrepancy with idealized vertical structure.**

HLCC in OFES / observations: viscosity or diffusion?

$$M_n = \frac{4R^2}{\pi^2 \sigma R_n^2}$$

$$\sigma \sim 10$$

$$R_1 \sim 60 \text{ km}$$

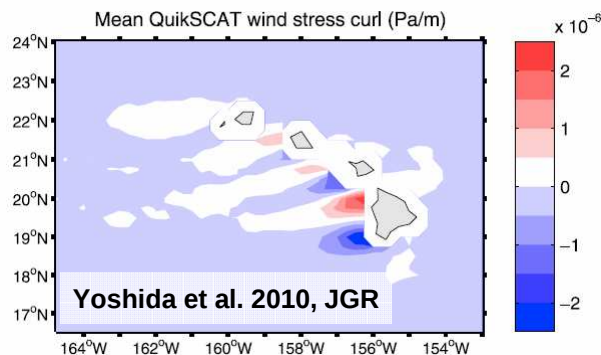


$$R \sim 200 \text{ km} \Rightarrow M_1 \sim 0.45$$

$$n_0 \sim 2$$

$$R \sim 100 \text{ km} \Rightarrow M_1 \sim 0.11$$

$$n_0 \sim 4$$



$$R \sim 40 \text{ km} \Rightarrow M_1 \sim 0.02$$

$$n_0 \sim 8$$

$$(ROMS) M_1 \sim 0.04$$

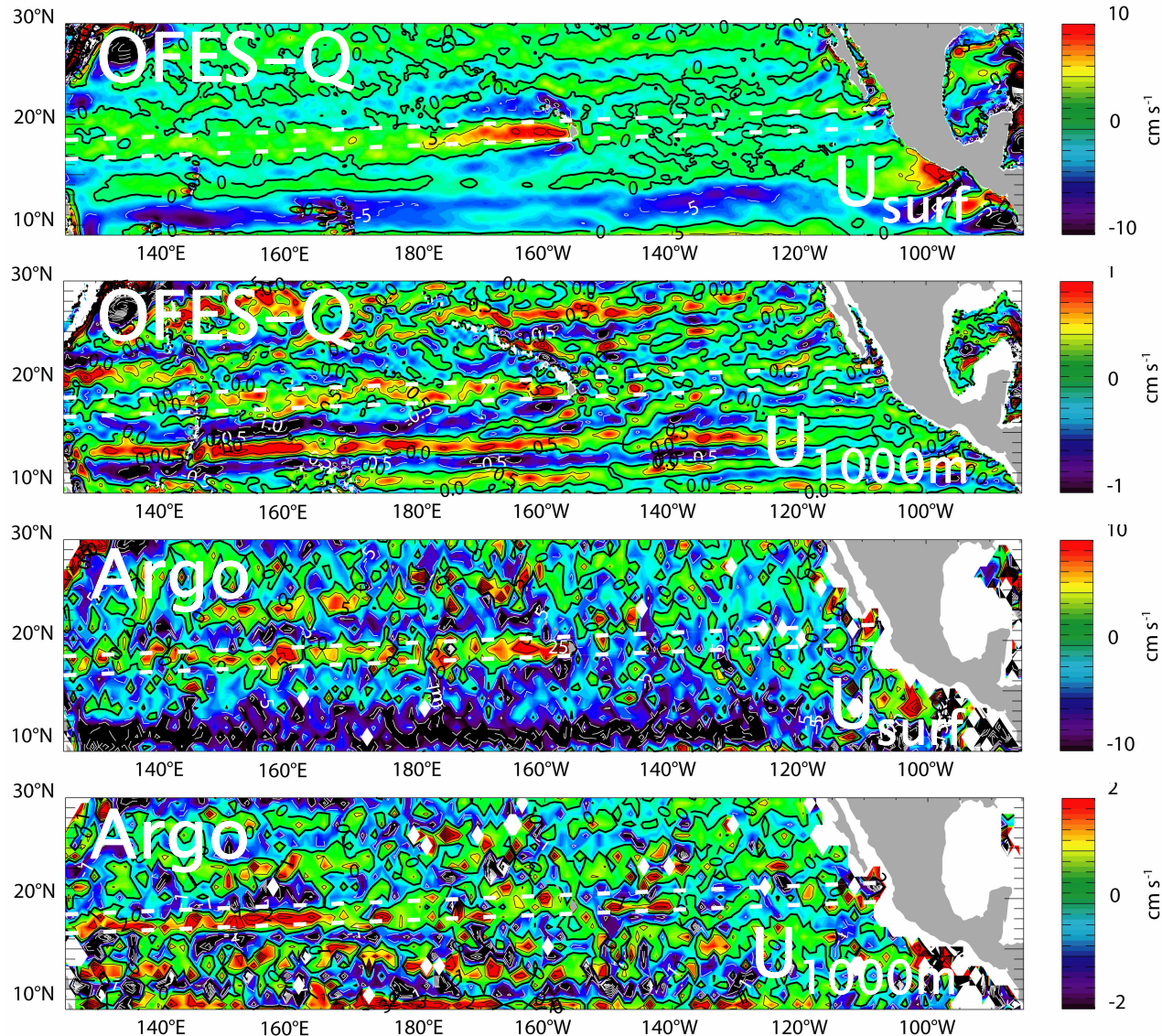
$$n_0 \sim 6$$

- Estimates derived from observed winds suggest **viscosity plays a significant role**.
- Wind and mixing in idealized runs are reasonable (perhaps even more than those in OFES).

HLCC in the real ocean?

(a)

Meridionally highpass filtered



Argo consistent w/ deepening:

- max near **Hawaii @ 0m**
- near **145-165°E @ 1000m**

Caution: scarce / noisy data...
but is the only available data!
(perhaps)

OFES-Q ≠ deep flow increase
but air-sea coupling may be
poorly represented

(Chelton Xie 2010)

Conclusion

- An idealized linear primitive-equation model and an analytical linear continuously-stratified model show that for **small-scale wind forcing**, **vertical viscosity** (and diffusion) **damps baroclinic Rossby waves**, resulting in a **β -plume westward thickening** with **decay of surface zonal jets** and **emergence of deep flow**. Barotropic flow is in Sverdrup balance and zonal transport is x-independent.
- **Zonal change** in baroclinic flow occurs over **shorter** (longer) **distances** for **smaller** (larger) **meridional forcing scales**, if forcing smaller than 1st Rossby radius.
- **Eddies** are not necessary for the early termination of β -plumes.

Conclusion (2)

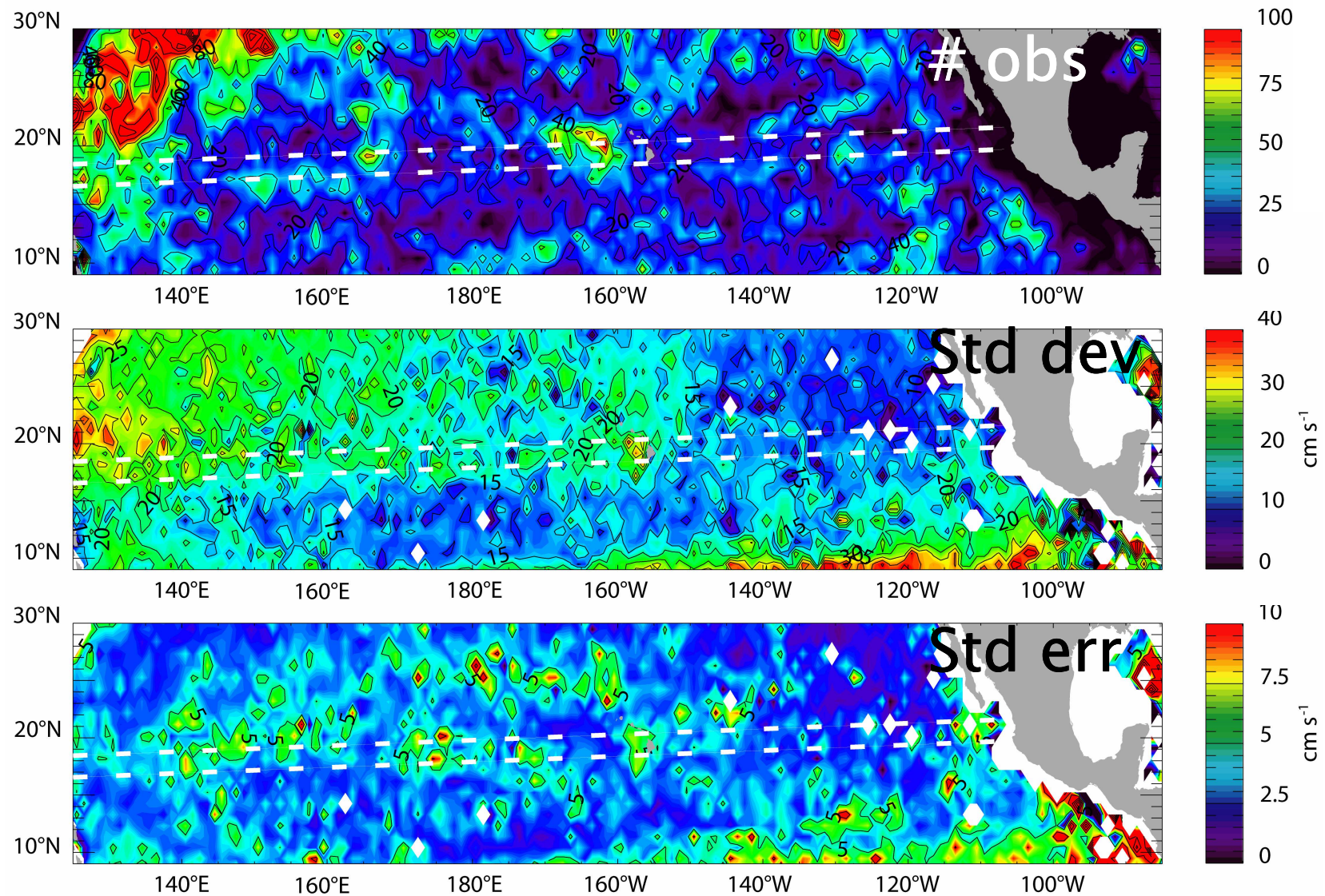
- High-resolution OGCM simulations suggest that the **Hawaiian Lee Countercurrent may have baroclinic and barotropic structures consistent with idealized linear β -plumes**. Model surface HLCC also has **similar sensitivity to scale of WSC** in lee of Hawaii.
- Specific roles of far-field **air-sea interaction** and **eddy fluxes** need to be addressed.
- **A possible deep extension of HLCC is found** for the first time in **ARGO float trajectory data** and in OGCM simulations.

Gracias!

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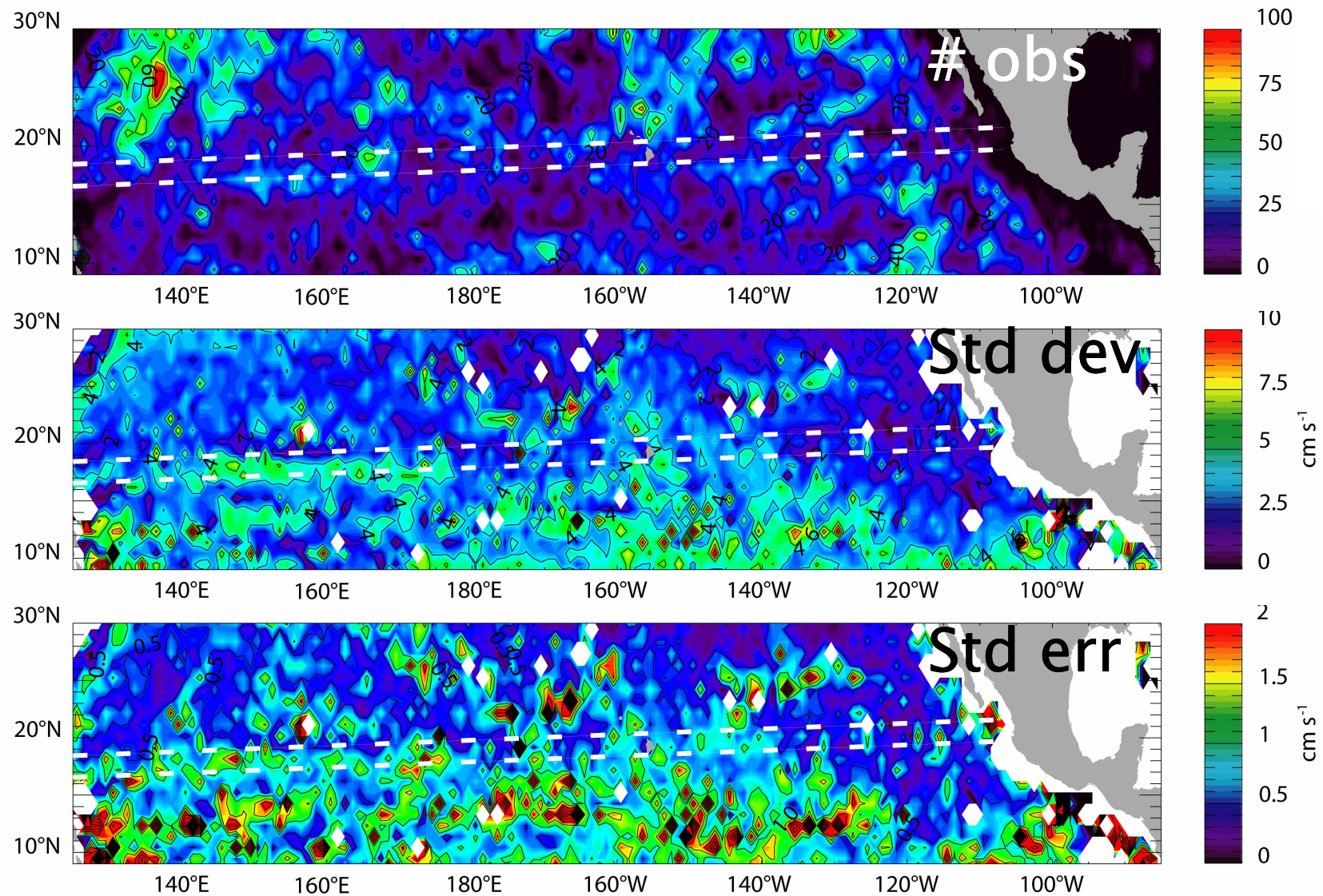
Standard error in Argo data @ 0 m

(a)

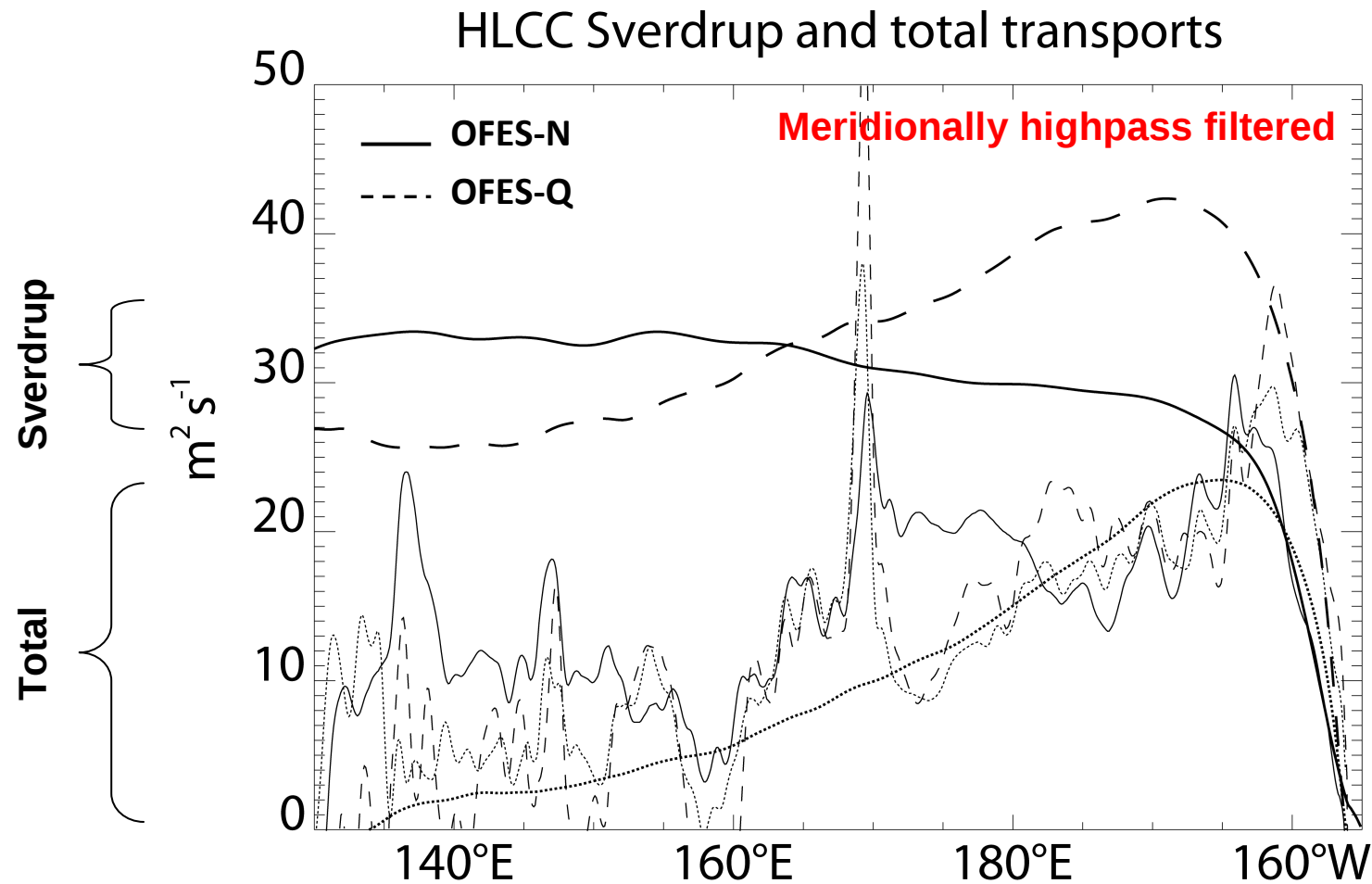


Standard error in Argo data @ 1000 m

(a)



Transport decay: Sverdrup flow?



- NCEP WSC favors an $\sim x$ -independent transport west of Hawaii, whereas **QuikSCAT WSC likely contributes to the faster-decaying transport.**
- This is likely due to the effect of **air-sea interaction** in the far field with **tilted WSC dipole and HLCC**. Possibly also contributes to **discrepancy with idealized vertical structure.**